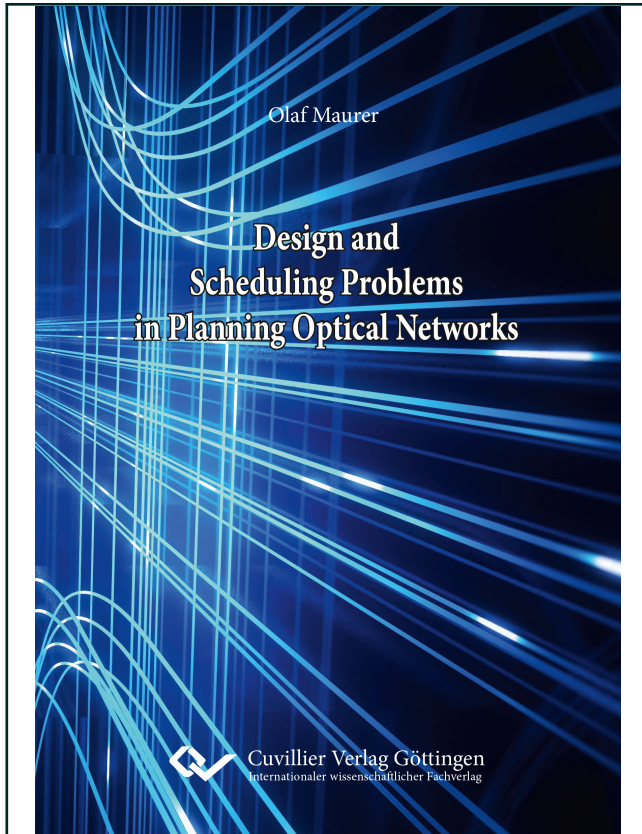




Olaf Maurer (Autor)

## **Design and Scheduling Problems in Planning Optical Networks**



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