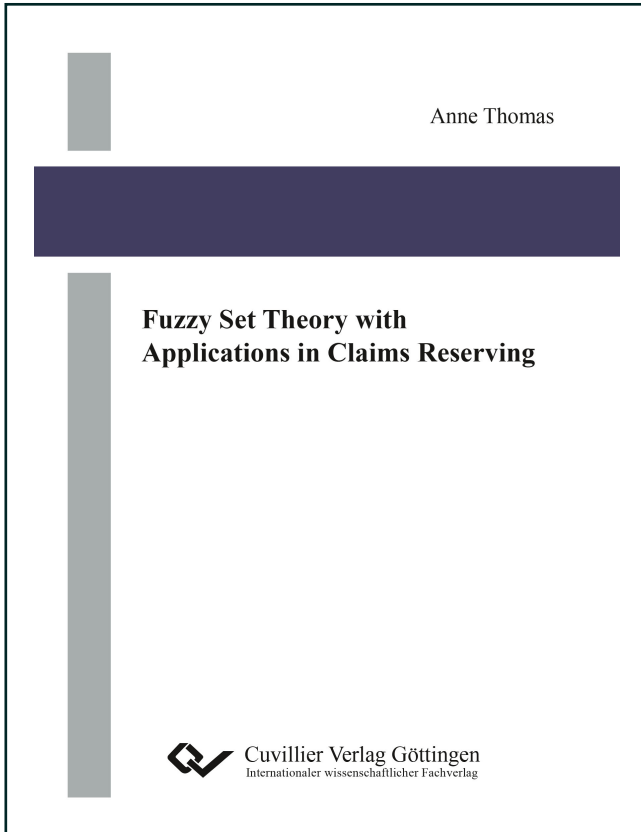




Anne Thomas (Autor)

Fuzzy Set Theory with Applications in Claims Reserving



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