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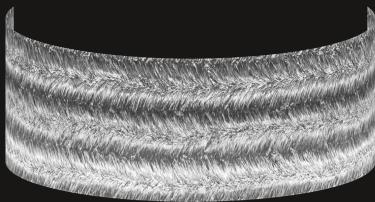
**Angular momentum transport and pattern formation  
in medium- and wide-gap turbulent Taylor-Couette  
flow**

An experimental study

Andreas Froitzheim

Angular momentum transport and pattern  
formation in medium- and  
wide-gap turbulent Taylor-Couette flow:

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