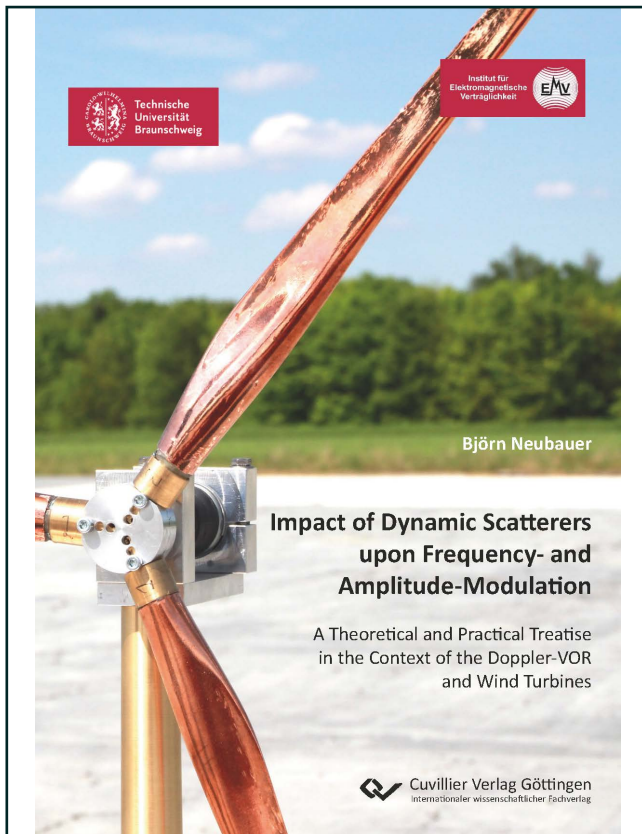




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Impact of Dynamic Scatterers upon Frequency- and Amplitude-Modulation

A Theoretical and Practical Treatise in the Context of the Doppler-VOR and Wind Turbines



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Contents

1. Prologue	1
1.1. Summing Two Oscillations of Equal Angular Velocity	1
1.2. Summing Two Oscillations of Different Angular Velocity	9
1.3. Technical Context	12
2. Doppler VOR - Function Principle	15
2.1. Composition of the DVOR Signal	17
3. Signal Deterioration of the FM-Component due to a Single, Static Scatterer	20
3.1. Three Approximations — Anderson et al.	20
3.2. One Approximation Only — This Work	33
3.3. Evaluation of (3.59) and its Comparison with Anderson’s Bearing Error (3.33) .	36
4. Signal Deterioration of the FM-Component due to a Stationary, Non-Static Scatterer	49
4.1. FM-Component — Impact of Time Varying Signal Strength and Constant Doppler Shift	49
4.2. Impact of Time Varying Signal Strength $A(t)$ and Time Varying Doppler Shift $\Delta\omega_2(t)$	64
5. Signal Deterioration of the AM-Component due to a Stationary, Non-Static Scatterer	70
5.1. Superposition of Two Amplitude Modulated Waves	70
5.2. Amplitude Modulated Signal Component	72
5.2.1. Static Scatterer	80
5.2.2. Superposition of an AM with an Amplitude Modulated AM without Doppler Shift	81
5.2.2.1. $\rho_A = +\rho$	82
5.2.2.2. $\rho_A = -\rho$	85
5.2.2.3. $\rho_A = 2\rho$	87
5.2.2.4. $\rho_A = -2\rho$	89
5.2.3. Phase Shift of an AM due to the Superposition with an Amplitude Modulated AM without Doppler Shift	91
5.2.3.1. Evaluation of the Phase Shift due to Resonant Modulating Angular Velocity ρ_A	91
5.2.3.2. Evaluation of the Phase Shift Due to an Arbitrary Modulating Angular Velocity ρ_A	101
5.3. Amplitude Modulation of the Second AM Signal, including Doppler Shift . . .	106
5.3.1. $AV_1 : \Delta\omega_1 \stackrel{!}{=} \rho$	107
5.3.1.1. $\Delta\omega_1 = \rho$ and $\rho_A = \rho$	107
5.3.2. $AV_2, AV_3 : \rho \mp \Delta\omega_1 \stackrel{!}{=} \rho$	109
5.3.3. $AV_4 : \rho_A - \Delta\omega_1 \stackrel{!}{=} \rho$	109
5.3.3.1. $a = 2, \Delta\omega_1 = 2\rho, \rho_A = 3\rho$	111
5.3.4. $AV_5 : \rho_A + \Delta\omega_1 \stackrel{!}{=} \rho$	113

5.3.5.	$AV_6, AV_9 : \rho \pm \rho_A \mp \Delta\omega_1 \stackrel{!}{=} \rho$	114
5.3.6.	$AV_7 : \rho + \rho_A + \Delta\omega_1 \stackrel{!}{=} \rho$	116
5.3.7.	$AV_8 : \rho - \rho_A - \Delta\omega_1 \stackrel{!}{=} \rho$	117
5.4.	Oscillating Doppler Shift: $\Delta\omega_1(t) = \Omega_{1,ds} \sin[\omega_{1,ds}t - \phi_{1,ds}]$	117
5.4.1.	$\cos[z \sin[\xi] + g] = \sum_{n=-\infty}^{\infty} J_n(z) \cos[n\xi + g]$	121
5.4.2.	$\cos[z \sin[\xi] + g]$ $= \cos[g]J_0(z) + 2 \cos[g] \sum_{n=1}^{+\infty} J_{2n}(z) \cos[2n\xi] - 2 \sin[g] \sum_{n=0}^{\infty} J_{2n+1}(z) \sin[(2n+1)\xi]$	124
5.5.	Determining the AM's Phase Deviation due to a Stationary Scatterer of Oscillating Character	127
6.	Assessment of the Remaining Approximation — Validity of the Derived Expressions	129
7.	Scaled Environment	132
8.	Measurement Concept and Hardware Setup	137
9.	Used Antennae	139
10.	Development and Evaluation of a Scaled Terrain Topology	143
10.1.	Height Scans	150
11.	Scaled Wind Turbines	160
12.	Measurements in a Triangular Alignment	165
12.1.	Scatterer induced Doppler Shifts	165
12.2.	Impact of a dynamic Scatterer Induced AM upon the DVOR-Signal — Generic Blades	177
12.3.	Impact of a Scatterer Induced AM upon the DVOR-Signal — Commercial Blades	193
12.3.1.	Plane of Rotation	194
12.3.2.	Emitter Height	196
12.3.3.	One and Three Wind Turbines on flat Ground and on Hill	197
12.3.4.	Evaluating the Size of Building Restricted Areas by varying Distances	200
12.3.5.	Overview	201
13.	Measurements in a Line of Sight Alignment	203
13.1.	Pitch	203
13.2.	Plane of Rotation	204
13.3.	Perpendicular Offset	205
13.4.	Wind Turbine Types	206
13.5.	Overview	209
14.	Summary	211
15.	Outlook	219
A.	Mathematical Appendix	221
A.1.	Euler Equation and Trigonometric Functions	221
A.2.	The Sign in The Angular Functions	221
A.3.	Sinus of Arc Cosine	221
A.4.	Addition Theorem	221

A.5. Addition Theorem II	222
A.6. Addition Theorem III	222
A.7. Tangent of the Sum and Difference of two Angles [6]: (2.87)	223
A.8. Extreme Value Problem of Subsection 1.2	224
A.9. Summation of two Oscillations	226
A.9.1. Summation of two Oscillations	229
A.10. Products of Trigonometric Functions [6]	231
A.10.1. Applying Identities on (4.23) yielding (4.24)	231
A.10.2. Applying (A.72) on (4.57)	232
A.10.3. Summation of (A.79) and (A.80)	232
A.11. Bessel Function	233
A.11.1. Bessel Function as Series	233
A.11.2. Identities for Negative Arguments	233
A.11.3. Bessel Function: Relation between J_n and J_{-n}	234
A.11.4. Derivation of the Bessel function	234
A.11.5. Series Expansion of the Angular Functions with Bessel Functions:	234
A.11.5.1. $e^{jz \sin[\xi]}$, $\sin[z \sin[\xi]]$, $\cos[z \sin[\xi]]$	234
A.11.5.2. $e^{jz \cos[\xi]}$, $\sin[z \cos[\xi]]$, $\cos[z \cos[\xi]]$ [7]	235
A.11.6. Extended Series Expansion of the Angular Functions with Bessel Functions	236
A.11.6.1. $\sin[z \sin[\xi] + g]$ and $\cos[z \sin[\xi] + g]$	237
A.11.6.2. $\sin[z \cos[\xi] + g]$ and $\cos[z \cos[\xi] + g]$	238
A.11.7. $\sin(z \sin(\xi) + g) = \sum_{-\infty}^{\infty} \dots$	240
A.11.8. $\cos(z \sin(\xi) + g) = \sum_{-\infty}^{\infty} \dots$	242
A.12. Trigonometric (Fourier) series	243
A.13. Arcus Function with a negative Argument	244
A.14. Derivation	244
A.14.1. Derivation of a Product of Three Functions	244
A.14.2. Chain Rule	244
A.15. Applying the addition theorems (A.70), (A.71) on the products of angular functions in (5.111)	244
A.15.1. $\cos[2n\xi] \cdot \cos[g_1]$	244
A.15.2. $\cos[2n\xi] \cdot \cos[g_2]$	245
A.15.3. $\cos[2n\xi] \cdot \cos[g_3]$	245
A.15.4. $\cos[2n\xi] \cdot \cos[g_4]$	246
A.15.5. $\cos[2n\xi] \cdot \cos[g_5]$	246
A.15.6. $\cos[2n\xi] \cdot \cos[g_6]$	247
A.15.7. $\cos[2n\xi] \cdot \cos[g_7]$	247
A.15.8. $\cos[2n\xi] \cdot \cos[g_8]$	247
A.15.9. $\cos[2n\xi] \cdot \cos[g_9]$	248
A.15.10. $\sin[(2n + 1)\xi] \cdot \sin[g_1]$	248
A.15.11. $\sin[(2n + 1)\xi] \cdot \sin[g_2]$	249
A.15.12. $\sin[(2n + 1)\xi] \cdot \sin[g_3]$	249
A.15.13. $\sin[(2n + 1)\xi] \cdot \sin[g_4]$	250
A.15.14. $\sin[(2n + 1)\xi] \cdot \sin[g_5]$	250
A.15.15. $\sin[(2n + 1)\xi] \cdot \sin[g_6]$	251
A.15.16. $\sin[(2n + 1)\xi] \cdot \sin[g_7]$	251
A.15.17. $\sin[(2n + 1)\xi] \cdot \sin[g_8]$	252
A.15.18. $\sin[(2n + 1)\xi] \cdot \sin[g_9]$	252

B. Physical Appendix	253
B.1. Doppler Effect	253
B.1.1. Doppler Effect for Electromagnetic Waves	253
B.1.2. Relativistic Effects?	254
B.1.3. Influence of the Scaling upon the Doppler Shift	256
B.2. Background Doppler Effect for electromagnetic Waves	258
B.2.0.1. Time Delitation	260
B.3. Dimensioning the DVOR-Radius	261
C. Case Distinctions Appendix — Phase Deviation of the AM Signal	262
C.1. AV_1	262
C.1.1. $\Delta\omega_1 = \rho$ and $\rho_A = -\rho$	262
C.1.2. $\Delta\omega_1 = \rho$ and $\rho_A = 2\rho$	264
C.2. $AV_2, AV_3 : \rho \mp \Delta\omega_1 \stackrel{!}{=} \rho$	265
C.3. $AV_4 : \rho_A - \Delta\omega_1 \stackrel{!}{=} \rho$	265
C.3.1. $a = 0, \Delta\omega_1 = 0, \rho_A = \rho$	265
C.3.2. $a = 0.5, \Delta\omega_1 = 0.5\rho, \rho_A = 1.5\rho$	265
C.3.3. $a = -0.5, \Delta\omega_1 = -0.5\rho, \rho_A = 0.5\rho$	267
C.3.4. $a = 1, \Delta\omega_1 = \rho, \rho_A = 2\rho$	269
C.3.5. $a = -1, \Delta\omega_1 = -\rho, \rho_A = 0$	270
C.3.6. $a = -1.5, \Delta\omega_1 = -1.5\rho, \rho_A = -0.5\rho$	271
C.3.7. $a = -2, \Delta\omega_1 = -2\rho, \rho_A = -\rho$	272
C.3.8. $a = 5, \Delta\omega_1 = 5\rho, \rho_A = 6\rho$	273
C.3.9. $a = -5, \Delta\omega_1 = -5\rho, \rho_A = -4\rho$	274
C.3.10. $a = 5, \Delta\omega_1 = 5\rho, \rho_A = 6\rho$	275
C.3.11. $a = 9.9, \Delta\omega_1 = 9.9\rho, \rho_A = 10.9\rho$	277
C.4. $AV_5 : \rho_A + \Delta\omega_1 \stackrel{!}{=} \rho$	278
C.4.1. $\tilde{a} = 0, \Delta\omega_1 = 0, \rho_A = \rho$	278
C.4.2. $\tilde{a} = 0.5, \Delta\omega_1 = 0.5\rho, \rho_A = 0.5\rho$	278
C.4.3. $\tilde{a} = -0.5, \Delta\omega_1 = -0.5\rho, \rho_A = 1.5\rho$	280
C.4.4. $\tilde{a} = 1, \Delta\omega_1 = \rho, \rho_A = 0$	282
C.4.5. $\tilde{a} = -1, \Delta\omega_1 = -\rho, \rho_A = 2\rho$	282
C.4.6. $\tilde{a} = 1.5, \Delta\omega_1 = 1.5\rho, \rho_A = -0.5\rho$	283
C.4.7. $\tilde{a} = 2, \Delta\omega_1 = 2\rho, \rho_A = -\rho$	285
C.4.8. $\tilde{a} = -2, \Delta\omega_1 = -2\rho, \rho_A = 3\rho$	286
C.4.9. $\tilde{a} = 5, \Delta\omega_1 = 5\rho, \rho_A = -4\rho$	287
C.4.10. $\tilde{a} = -5, \Delta\omega_1 = -5\rho, \rho_A = 6\rho$	289
C.4.11. $\tilde{a} = 9.9, \Delta\omega_1 = 9.9\rho, \rho_A = -8.9\rho$	290
C.4.12. $\tilde{a} = -9.9, \Delta\omega_1 = -9.9\rho, \rho_A = 10.9\rho$	291
C.5. $AV_6, AV_9 : \rho \pm \rho_A \mp \Delta\omega_1 \stackrel{!}{=} \rho$	292
C.5.1. $\check{a} = 0, \Delta\omega_1 = \rho_A = 0$	292
C.5.2. $\check{a} = 0.5, \Delta\omega_1 = \rho_A = 0.5\rho$	294
C.5.3. $\check{a} = -0.5, \Delta\omega_1 = \rho_A = -0.5\rho$	297
C.5.4. $\check{a} = 1, \Delta\omega_1 = \rho_A = \rho$	299
C.5.5. $\check{a} = -1, \Delta\omega_1 = \rho_A = -\rho$	301
C.5.6. $\check{a} = 2, \Delta\omega_1 = \rho_A = 2\rho$	302
C.5.7. $\check{a} = -2, \Delta\omega_1 = \rho_A = -2\rho$	303
C.5.8. $\check{a} = 5, \Delta\omega_1 = \rho_A = 5\rho$	305
C.5.9. $\check{a} = -5, \Delta\omega_1 = \rho_A = -5\rho$	306

C.6.	$AV_7: \rho + \rho_A + \Delta\omega_1 \stackrel{!}{=} \rho$	307
C.6.1.	$\acute{a} = 0, \Delta\omega_1 = 0, \rho_A = 0$	307
C.6.2.	$\acute{a} = 0.5, \Delta\omega_1 = 0.5\rho, \rho_A = -0.5\rho$	308
C.6.3.	$\acute{a} = -0.5, \Delta\omega_1 = -0.5\rho, \rho_A = 0.5\rho$	311
C.6.4.	$\acute{a} = 1, \Delta\omega_1 = \rho, \rho_A = -\rho$	313
C.6.5.	$\acute{a} = -1, \Delta\omega_1 = -\rho, \rho_A = \rho$	314
C.6.6.	$\acute{a} = 2, \Delta\omega_1 = 2\rho, \rho_A = -2\rho$	315
C.6.7.	$\acute{a} = -2, \Delta\omega_1 = -2\rho, \rho_A = 2\rho$	317