



Cristóbal Tapia Camú (Autor)

## **Variation of mechanical properties in oak boards and its effect on glued laminated timber**

Application to a stochastic finite element glulam strength model

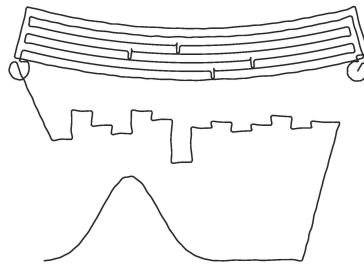


Universität Stuttgart

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Internationaler wissenschaftlicher Fachverlag

<https://cuvillier.de/de/shop/publications/8616>

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# CONTENTS

<b>1</b>	<b>Introduction</b>	<b>17</b>
1.1	European forests in the 21 <sup>st</sup> century . . . . .	17
1.2	Hardwoods in the building industry . . . . .	19
1.3	Glued laminated timber . . . . .	20
1.3.1	Characterization of mechanical properties of glulam according to EN 14080 . . . . .	22
1.3.2	Towards standardization of hardwood GLT . . . . .	23
1.3.3	The example of softwoods: strength models . . . . .	24
1.4	Objectives . . . . .	25
1.5	Scope . . . . .	26
1.6	Outline and overview . . . . .	26
<b>2</b>	<b>State of the art</b>	<b>27</b>
2.1	General remarks . . . . .	27
2.2	A look at the variation in wood: sources of uncertainty . . . . .	27
2.3	General statistical concepts and methods for the analysis of wood properties . . . . .	30
2.3.1	Weibull theory of weakest link . . . . .	30
2.3.2	Order statistics and extreme value theory . . . . .	31
2.3.3	Survival analysis . . . . .	31
2.4	Probabilistic methods for the simulation of correlated variables . . .	33

2.4.1	Simulation of correlated normally distributed variables . . . . .	33
2.4.2	Simulation of correlated non-normally distributed variables . . . . .	34
2.4.3	Autoregressive models . . . . .	34
2.5	Models for the simulation of material properties along boards . . . . .	36
2.5.1	Predictor-based stochastic models . . . . .	38
2.5.2	Pure stochastic models . . . . .	40
2.5.3	Simulation of KAR values along the boards . . . . .	47
2.6	Probabilistic strength models for glulam beams . . . . .	48
2.6.1	Model by Foschi and Barrett (1980) . . . . .	48
2.6.2	Karlsruher Rechenmodel . . . . .	49
2.6.3	PROLAM model . . . . .	50
2.6.4	Karlsruher Rechenmodel (latest implementation) . . . . .	51
2.6.5	Model by Fink (2014) . . . . .	52
2.6.6	Model by Kandler et al. (2018) . . . . .	53
<b>3</b>	<b>Materials</b> . . . . .	<b>55</b>
3.1	General remarks . . . . .	55
3.2	Dataset A: Material used for the study of within board variation . . . . .	56
3.2.1	Segmentation of boards . . . . .	57
3.2.2	Grain deviation . . . . .	58
3.2.3	Knot-related variables . . . . .	58
3.2.4	Dynamic modulus of elasticity measurements . . . . .	58
3.3	Dataset B: Glulam experimental data: Gamiz . . . . .	59
3.3.1	Mechanical properties of boards . . . . .	60
3.3.2	Mechanical properties of glulam beams . . . . .	61
3.3.3	Distribution of board lengths in glulam . . . . .	62
3.4	Dataset C: FCBA experimental campaign . . . . .	62
3.4.1	Mechanical properties of boards and finger-joints . . . . .	62
3.4.2	Mechanical properties of glulam beams . . . . .	63

<b>4 Analysis of knots in oak boards</b>	<b>65</b>
4.1 General Remarks . . . . .	65
4.2 Knot area ratios (KAR) . . . . .	66
4.2.1 Digitally reconstructing the 3D knot geometry of boards . .	67
4.2.2 Comparison of different KAR definitions . . . . .	68
4.2.3 KAR distributions . . . . .	72
4.3 Length of clear wood segments . . . . .	77
4.3.1 Definition of clear wood length . . . . .	77
4.3.2 Clear wood length analysis . . . . .	78
4.4 Final remarks . . . . .	79
<b>5 Variation of mechanical properties in oak boards</b>	<b>81</b>
5.1 General . . . . .	81
5.2 Description of the experimental campaign . . . . .	82
5.2.1 Variation of modulus of elasticity along board . . . . .	82
5.2.2 Multiple tensile strength measurements . . . . .	83
5.2.3 Density measurements along boards . . . . .	85
5.3 Density variation within boards . . . . .	86
5.4 Modulus of elasticity . . . . .	88
5.4.1 Processing of measured data . . . . .	88
5.4.2 Global and local moduli of elasticity . . . . .	88
5.4.3 Correlation of MOE with density and KAR . . . . .	93
5.4.4 Normalization of the measured MOE data . . . . .	94
5.4.5 Transformation of normalized MOE to stationary data . .	98
5.4.6 Serial correlation of localized MOE measurements . . . .	99
5.5 Tensile strength . . . . .	104
5.5.1 Fracture behavior and global tensile strength . . . . .	105
5.5.2 Local tensile strength . . . . .	106
5.5.3 Relationship between tensile strength and MOE . . . . .	107
5.5.4 Estimation of the intra-board tensile strength distribution .	109

5.6	Regression models for MOE and $f_{t,0}$ . . . . .	117
5.7	Summary and discussion . . . . .	120
<b>6</b>	<b>Simulation of mechanical properties along oak boards</b>	<b>123</b>
6.1	General remarks . . . . .	123
6.2	Simulation of global properties of boards . . . . .	124
6.3	Localized modulus of elasticity . . . . .	125
6.3.1	Determination of order and parameters of the stationary AR process . . . . .	127
6.3.2	Model for the simulation of MOE profiles . . . . .	128
6.3.3	Example of simulations of MOE profiles along boards . . . . .	129
6.3.4	Consideration of different board lengths . . . . .	133
6.4	Localized tensile strength . . . . .	134
6.4.1	Model for the simulation of tensile strength profiles . . . . .	135
6.4.2	Simulation examples of tensile strength profiles along boards	136
6.4.3	Simulation of length effect for tensile strength . . . . .	137
6.4.4	Correlation of MOE and tensile strength at global level . . . . .	141
6.5	Localized compressive strength . . . . .	142
6.6	Discussion . . . . .	142
<b>7</b>	<b>Finite element model for the prediction of bending strength in glulam beams</b>	<b>145</b>
7.1	General remarks . . . . .	145
7.2	Input parameters . . . . .	146
7.2.1	Configuration files and hashing of parameters . . . . .	148
7.3	Finite element model . . . . .	148
7.3.1	Geometry and build-up characteristics . . . . .	151
7.3.2	Material properties . . . . .	152
7.3.3	Material assignment and meshing . . . . .	157
7.3.4	Boundary conditions . . . . .	159
7.3.5	Solver configuration . . . . .	160

7.4	Typical solution and post-processing of results . . . . .	161
7.4.1	General failure behavior . . . . .	161
7.4.2	Data extraction from the FE model . . . . .	163
7.4.3	Definition of bending failure . . . . .	163
7.5	Discussion . . . . .	164
<b>8</b>	<b>Model calibration and parametric analysis</b>	<b>165</b>
8.1	General remarks . . . . .	165
8.2	Studied configurations . . . . .	166
8.2.1	Dataset B . . . . .	166
8.2.2	Dataset C . . . . .	167
8.3	Analysis of stiffness results . . . . .	168
8.3.1	Stiffness results of dataset B . . . . .	168
8.3.2	Stiffness results of dataset C . . . . .	169
8.4	Calibration of fracture energy . . . . .	169
8.4.1	Calibration of fracture energies with dataset B . . . . .	170
8.4.2	Application of fitted energy values to dataset C . . . . .	173
8.5	Parametric analysis . . . . .	174
8.5.1	Effect of tensile strength distribution . . . . .	174
8.5.2	Effect of length of boards . . . . .	176
8.5.3	Effect of tensile strength of finger-joints . . . . .	179
8.6	Discussion . . . . .	185
<b>9</b>	<b>Conclusions and outlook</b>	<b>187</b>
9.1	Conclusions . . . . .	187
9.2	Outlook . . . . .	189
<b>References</b>		<b>191</b>
<b>List of Symbols</b>		<b>203</b>
<b>Appendix A Variation of MOE along boards</b>		<b>209</b>
<b>CONTENTS</b>		<b>7</b>

<b>Appendix B Analysis of MOE normalization method</b>	<b>217</b>
<b>Appendix C Testing of the user-defined material in a one-element problem</b>	<b>219</b>
<b>Appendix D Input parameters used in the strength model</b>	<b>221</b>
D.1 Parameters used for the strength model with dataset B . . . . .	221
D.2 Parameters used for the strength model with dataset C . . . . .	222
<b>Appendix E Reordering of vectors to maintain global correlation</b>	<b>223</b>