



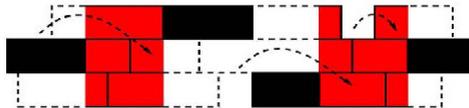
Marc Uetz (Autor)  
**Algorithms for Deterministic and Stochastic  
Scheduling**

Marc Uetz

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Stochastic Scheduling**

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