

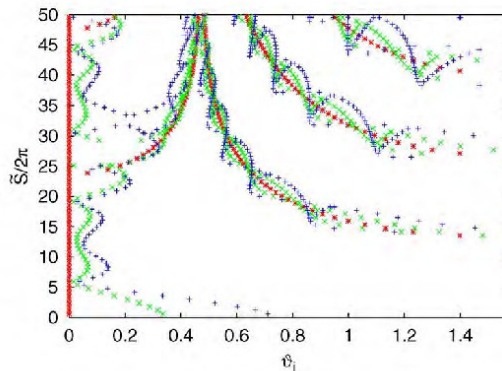


Thomas Bartsch (Autor)

The hydrogen atom in an electric field and in crossed electric and magnetic fields: Closed-orbit theory and semiclassical quantization

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