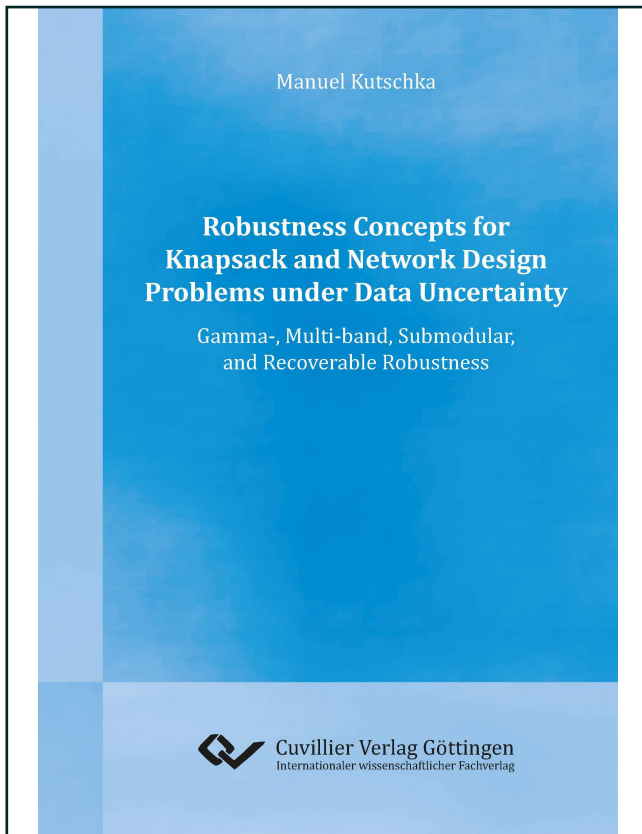




Manuel Kutschka (Autor)

**Robustness Concepts for Knapsack and Network
Design Problems under Data Uncertainty**

Gamma-, Multi-band, Submodular, and Recoverable
Robustness



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