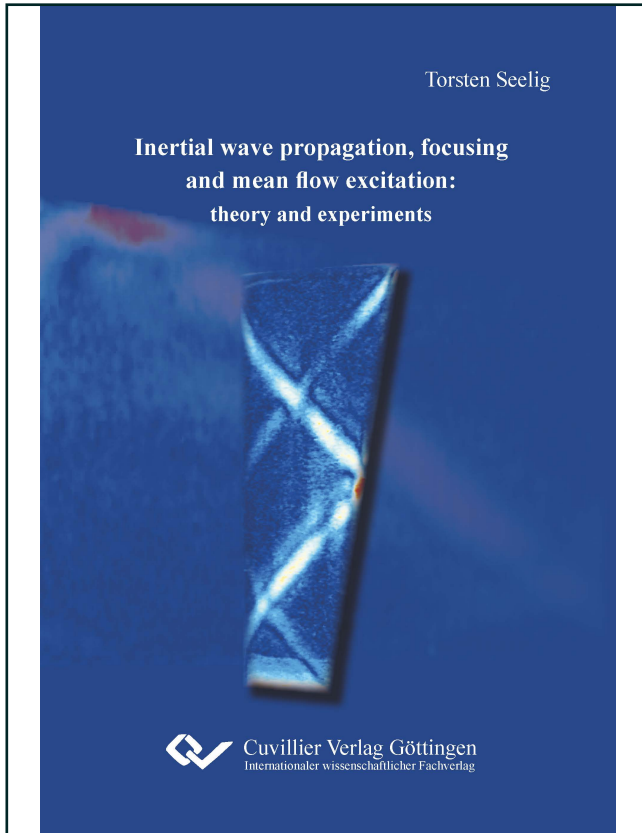




Torsten Seelig (Autor)

**Inertial wave propagation, focusing and mean flow
excitation**
theory and experiments



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